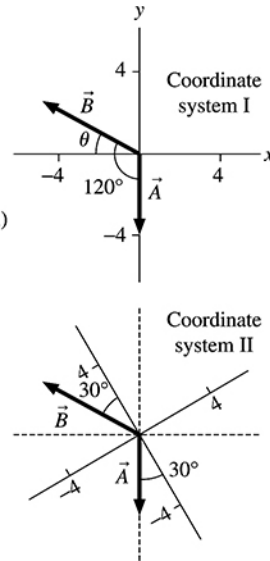


3.18. Visualize:

Known
 $\vec{A} = (4.0 \text{ m, vertically downward})$
 $\vec{B} = (5.0 \text{ m, } 60^\circ \text{ counterclockwise from vertical})$
 $\theta = 30^\circ$

Find
 A_x A_y B_x B_y in coordinate systems I and II



Solve: In coordinate system I, $\vec{A} = -(4 \text{ m})\hat{j}$, so $A_x = 0 \text{ m}$ and $A_y = -4 \text{ m}$. The vector \vec{B} makes an angle of 60° counterclockwise from vertical, which makes it have an angle of $\theta = 30^\circ$ with the $-x$ -axis. Since \vec{B} points to the left and up, it has a negative x -component and a positive y -component. That is, $B_x = -(5.0 \text{ m})\cos 30^\circ = -4.3 \text{ m}$ and $B_y = +(5.0 \text{ m})\sin 30^\circ = 2.5 \text{ m}$. Thus, $\vec{B} = -(4.3 \text{ m})\hat{i} + (2.5 \text{ m})\hat{j}$.

In coordinate system II, \vec{A} points to the left and down, and makes an angle of 30° with the $-y$ -axis. Therefore, $A_x = -(4.0 \text{ m})\sin 30^\circ = -2.0 \text{ m}$ and $A_y = -(4.0)\cos 30^\circ = -3.5 \text{ m}$. This implies $\vec{A} = -(2.0 \text{ m})\hat{i} - (3.5 \text{ m})\hat{j}$. The vector \vec{B} makes an angle of 30° with the $+y$ -axis and is to the left and up. This means we have to manually insert a minus sign with the x -component. $B_x = -B \sin 30^\circ = -(5.0 \text{ m})\sin 30^\circ = -2.5 \text{ m}$, and $B_y = +B \cos 30^\circ = (5.0 \text{ m})\cos 30^\circ = 4.3 \text{ m}$. Thus $\vec{B} = -(2.5 \text{ m})\hat{i} + (4.3 \text{ m})\hat{j}$.